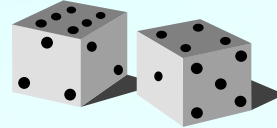


## A Randomize Protocol for Consensus

A complete network graph (clique)  
 $n$  - total number of processes.  
 $f$  - total number of faulty processes.  
Assumption:  $n > 5f$ .



This algorithm solves a more complex problem where the failure model is **Byzantine**, i.e. the failed processes can send arbitrary messages to arbitrary processes (may lie), or may fail.



## The protocol (Ben-Or variation)

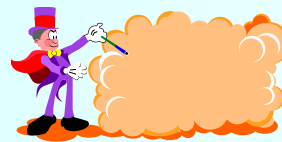
Round=0;  $x$  = initial value

Do **Forever**:

    Round = Round + 1

    Step 1

    Step 2



Step 1:

    Send **Proposal(Round, $x$ )** to all processes

    wait for  $n-f$  messages of type **Proposal(Round, $*$ )**

    if at least  $n-2f$  messages have the same value  $v$

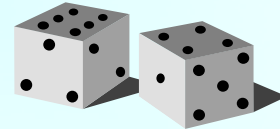
        then  $x = v$  (that value)

        else  $x = \text{undefined}$

## The Protocol (cont.)

### Step 2:

Send  $\text{Bid}(\text{Round}, x)$  to all processes  
wait for  $n-f$  messages of type  $\text{Bid}(\text{Round}, *)$   
 $v$  is the real value (0/1) occurring most often  
and  $m$  is the number of occurrences of  $v$   
if  $m \geq 3f+1$   
    then **Decide** ( $x=v$ )  
else if  $m \geq f+1$   
    then  $x = v$   
else  $x = \text{random}$  (0 or 1)



Submission: Thursday, October 27 at the beginning of class.  
Solution must be typed. No collaboration is allowed.

## Homework

1. Prove that the protocol in pages 20-22 is correct.  
i.e. that it satisfies the agreement, validity and  
termination (**with probability 1**) requirements.  
Termination means - **for reaching a decision**.  
**Assume at most  $f$  Byzantine failures.**

The communication is reliable FIFO unicast,  
although messages from different processes can  
arrive in different order to different processes.

2. (**only 437**) Modify the algorithm so that  
eventually, all non faulty processes that decide also halt.  
Try to make the modification as simple as possible.